

# Practical Design to Eurocode 2


The webinar will start at 12.30



## Course Outline


Lecture	Date	Speaker	Title
1	21 Sep	Jenny Burrridge	Introduction, Background and Codes
2	28 Sep	Charles Goodchild	EC2 Background, Materials, Cover and effective spans
3	5 Oct	Paul Gregory	Bending and Shear in Beams
4	12 Oct	Charles Goodchild	Analysis
5	19 Oct	Paul Gregory	Slabs and Flat Slabs
6	26 Oct	Charles Goodchild	Deflection and Crack Control
7	2 Nov	Jaylina Rana	Columns
8	9 Nov	Jenny Burrridge	Fire
9	16 Nov	Paul Gregory	Detailing
10	23 Nov	Jenny Burrridge	Foundations





# Introduction, Background and Codes

Lecture 1  
21<sup>st</sup> September 2017



## Summary: Lecture 1

- Introduction
- Background & Basics
- Eurocode (Eurocode 0)
- Eurocode Load Combinations
- Eurocode 2 Load Cases
- Eurocode 1 Loads/Actions
- Exercise





# Introduction



## Practical Design to Eurocode 2

### Objectives:


Starting on 21st September 2017, this ten-week (Thursday lunchtime) online course will cover the relevant sections of Eurocode 2, etc ; considering the practical application of the code with worked examples and hands-on polls and workshops on design.

The most common structural elements will be covered. The course is designed for practising UK engineers so will use the UK's Nationally Determined Parameters.

Following this course delegates will:


- Know your way around Eurocode 2: Parts 1-1 & 1-2, General design rules and fire design.
- Understand the context for the code, and the essential differences between Eurocode 2 and BS 8110 in practice.
- Have experience in design to Eurocode 2 requirements.
- Have experience using the code through worked examples






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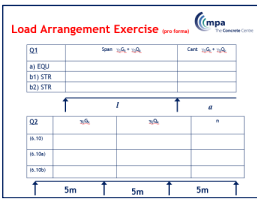


# Course Resources (soft copies)

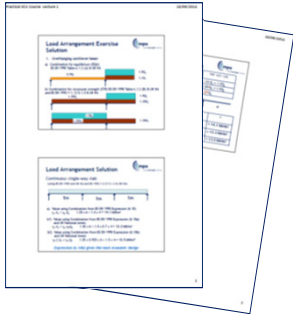
## Course notes



## Pro formas for exercises (as and when)



## Model answers (as and when)





## Course Resources (soft copy)





### Concise Eurocode 2

- Introduction Basis of Design
- Materials
- Durability and Cover
- Structural Analysis
- Bending and Axial Force
- Shear
- Punching Shear
- Torsion
- Serviceability
- Detailing - general
- Detailing - particular
- Tying systems
- Plain concrete
- Design Aids

Print this one out (or buy a copy!)

Lots of references to it later.

## Course Resources (soft copies)



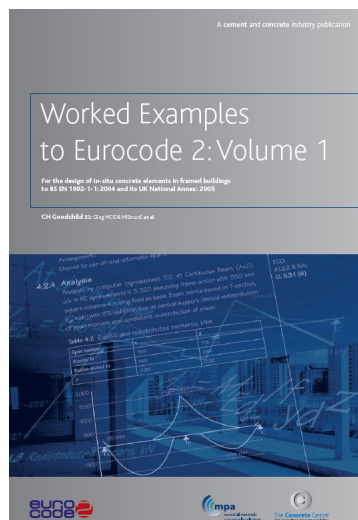


and/  
or





## Course Resources (soft copy)



### Worked Examples

- Introduction
- Analysis, actions and load arrangements
- Slabs (one-way and flat slabs)
- Beams
- Columns
- Walls
- Annex A: Derived Formulae
- Annex B: Serviceability Limit State
- Annex C: Design Aids

## Course Resources (soft copy)



### How to...Compendium


- Introduction to Eurocodes
- Getting started
- Slabs
- Beams
- Columns
- Foundations
- Flat slabs
- Deflections
- Retaining walls
- Detailing
- BS 8500
- Structural fire design



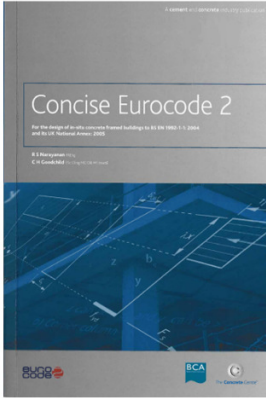
Revised Edition January 2011



## Go To Training - Control Panel

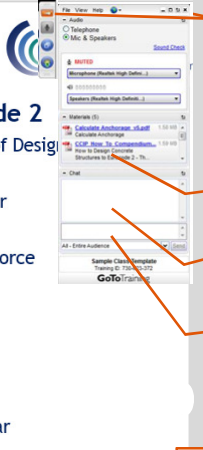
 The Concrete Centre

### Course Resources (soft copy)



#### Concise Eurocode 2

- Introduction Basis of Design
- Materials
- Durability and Cover
- Structural Analysis
- Bending and Axial Force
- Shear
- Punching Shear
- Torsion
- Serviceability
- Detailing - general
- Detailing - particular
- Tying systems
- Plain concrete
- Design Aids



**Show/Hide control panel**


**Materials**

**Chat: ask questions here**

**Chat**

**Session recordings will be sent after about 2 hours. Other issues: email Patience.**

## Go To Training - Polls

 The Concrete Centre

**QUICKPOLL**

One of the most stylish batsmen of his generation D.I.Gower played 117 test for England. What do the initials D I stand for?

Please select one:

- ☐ Glenn McGrath
- ☐ James Anderson
- ☐ David Ivon
- ☐ Muttiah Muralitharan

Organizers and Panelists don't vote.

**Poll Open**  
Poll can be closed by organizer

**QUICKPOLL**

One of the most stylish batsmen of his generation D.I.Gower played 117 test for England. What do the initials D I stand for?

Poll Results (single answer required):

Glenn McGrath	0%
James Anderson	0%
David Ivon	100%
Muttiah Muralitharan	0%

**Sharing Poll Results**  
Share the results with your audience



## Conventions:



From EN1992-1-1

From UK NA

TCC Comment

### Subscripts:

- E effects of actions
- R resistance
- d design value
- k characteristic value
- w shear

## Warning: Eurocode-speak!



letter	name	capita
α	Alpha	A
β	Beta	B
γ	Gamma	Γ
δ	Delta	Δ
ε	Epsilon	E
ζ	Zeta	Z
η	Eta	H
θ	Theta	Θ
ι	Iota	I
κ	Kappa	K
λ	Lambda	Λ
μ	Mu	M
ν	Nu	N
ξ	Xi	Ξ
ο	Omicron	O
π	Pi	Π
ρ	Rho	P
σ	Sigma	Σ
τ	Tau	T
υ	Upsilon	Υ
φ	Phi	Φ
χ	Chi	X
ψ	Psi	Ψ
ω	Omega	Ω

### Greek Alphabet

### Eurospeak

e.g:  
 Verify (check)  
 Action (load)  
*Variable* action (live load)  
*Permanent* action (dead load)  
*Frequent* value (for SLS checks)  
*Quasi-permanent* value (for long term SLS)  
 Annex (appendix)

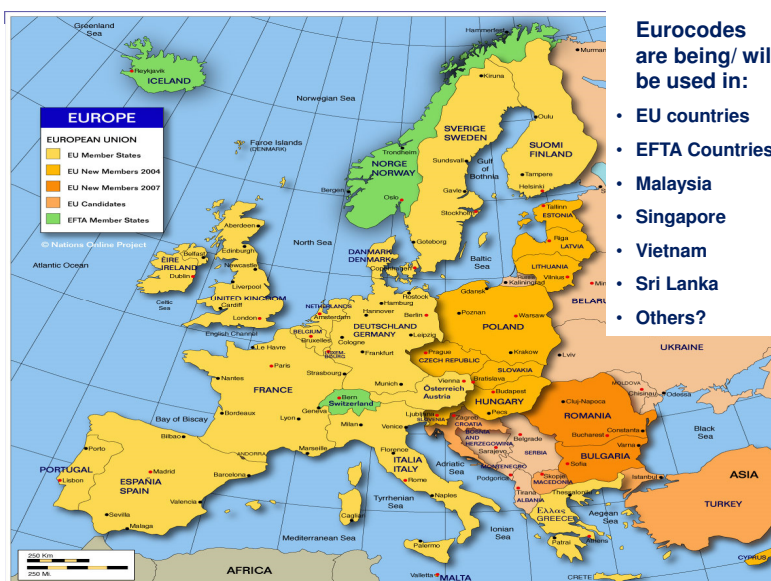


## Background & Basics

### Setting the scene

#### CEN National Members

Austria Belgium  
 Cyprus  
 Czech Republic  
 Denmark  
 Estonia Finland  
 France  
 Germany  
 Greece Hungary  
 Iceland Ireland  
 Italy Latvia  
 Lithuania  
 Luxembourg  
 Malta  
 The Netherlands  
 Norway Poland  
 Portugal  
 Romania  
 Slovakia  
 Slovenia Spain  
 Sweden  
 Switzerland  
 United Kingdom



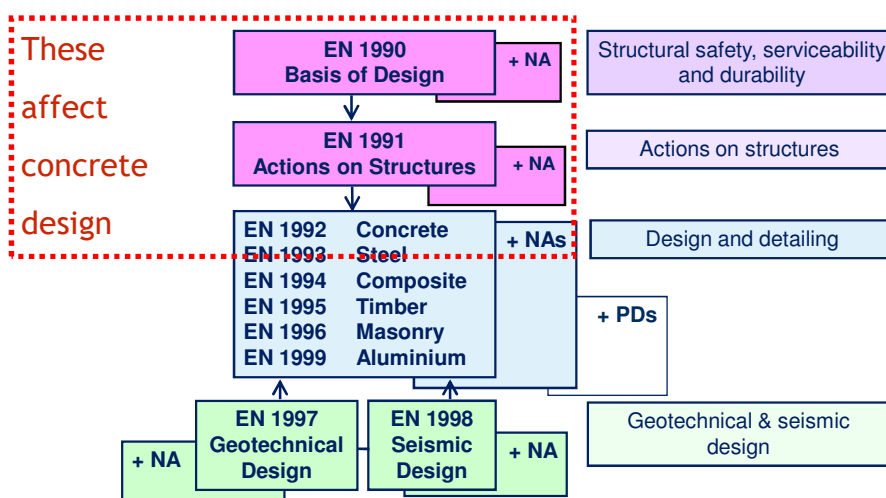


## The Eurocodes



- BS EN 1990 (EC0) : Basis of structural design
- BS EN 1991 (EC1) : Actions on Structures
- BS EN 1992 (EC2) : Design of concrete structures
- BS EN 1993 (EC3) : Design of steel structures
- BS EN 1994 (EC4) : Design of composite steel and concrete structures
- BS EN 1995 (EC5) : Design of timber structures
- BS EN 1996 (EC6) : Design of masonry structures
- BS EN 1997 (EC7) : Geotechnical design
- BS EN 1998 (EC8) : Design of structures for earthquake resistance
- BS EN 1999 (EC9) : Design of aluminium structures

## Eurocode Hierarchy



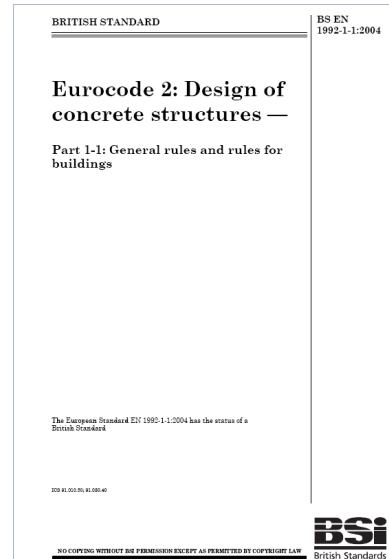


## Format of the Eurocodes



## Each Eurocode Contains:

- National front cover

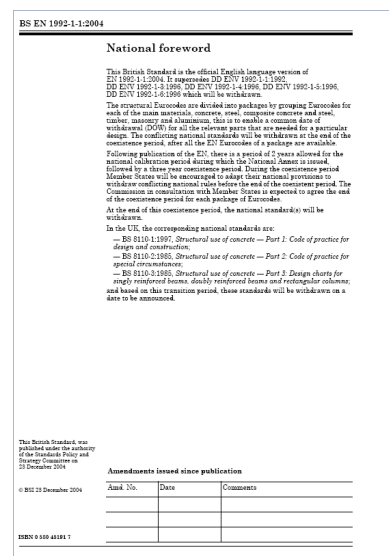


## Format of the Eurocodes



### Each Eurocode Contains:

- National front cover
- National foreword



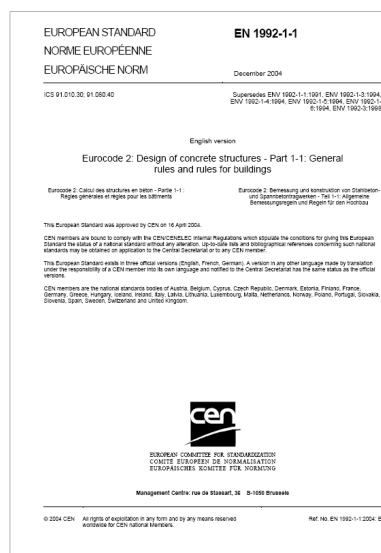


## Format of the Eurocodes



### Each Eurocode Contains:

- National front cover
- National foreword
- CEN front cover

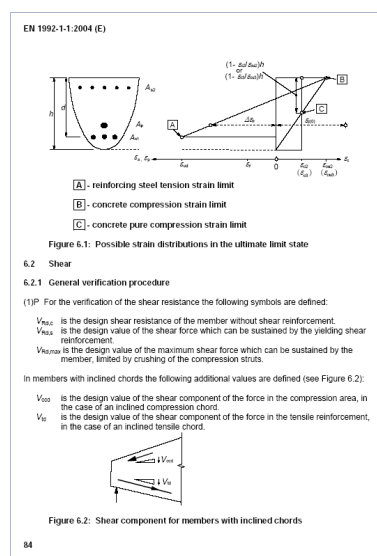


## Format of the Eurocodes



### Each Eurocode Contains:

- National front cover
- National foreword
- CEN front cover
- Main text and annexes (which must be as produced by CEN)





## Format of the Eurocodes



### Each Eurocode Contains:

- National front cover
- National foreword
- CEN front cover
- Main text and annexes (which must be as produced by CEN)
- Annexes - can be normative and/or informative

EN 1992-1-1:2004 (E)

ANNEX C (Normative)

Properties of reinforcement suitable for use with this Eurocode

C.1 General

(1) Table C.1 gives the properties of reinforcement suitable for use with this Eurocode. The properties are valid for temperatures between -40°C and 100°C for the reinforcement in the finished structure. Any bending and welding of reinforcement carried out on site should be further restricted to the temperature range as permitted by EN 13670.

Table C.1: Properties of reinforcement

Product form	Bars and de-coiled rods			Wire Fabrics			Requirement or quality value (%)
Class	A	B	C	A	B	C	
Characteristic yield strength $f_{yk}$ or $f_{yk}$ (MPa)	400 to 600						5.0
Minimum value of $k = f_{yk}/f_{yk}$	21.05	21.06	21.15 -1.35	21.05	21.06	21.15 -1.35	10.0
Characteristic strain at maximum force, $\epsilon_{yk}$ (%)	22.5	23.0	27.5	22.5	23.0	27.5	10.0
Bendability	Bend/Rebend test						
Shear strength	0.3 $f_{yk}$ (in area of stirr.)						Minimum
Maximum deviation from nominal mass (individual bar or wire) (%)	± 5						5.0

Note: The values for the fatigue stress range with an upper limit of  $f_{yk}$  and for the Minimum relative rib area for use in a Country may be found in its National Annex. The recommended values are given in Table C.2N. The value of  $d$  for use in a Country may be found in its National Annex. The recommended value is 0.6.

Table C.2N: Properties of reinforcement

Product form	Bars and de-coiled rods			Wire Fabrics			Requirement or quality value (%)
Class	A	B	C	A	B	C	
Fatigue stress range (MPa) for $N \geq 2 \times 10^6$ cycles with an upper limit of $f_{yk}$	210			210			10.0
Bond	Nominate bar size (mm)						
Minimum relative rib area	1 to 1.5 to 12						5.0
Max. $f_{yk}$	0.055						
Max. $f_{yk}$	0.060						
Max. $f_{yk}$	0.066						

Fatigue: Exceptions to the fatigue rules for use in a Country may be found in its National Annex. The

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## Format of the Eurocodes



### National Annex (NA)

Table NA.1 — UK decisions for Nationally Determined Parameters described in BS EN 1992-1-1:2004 (continued)

Subclause	Nationally Determined Parameter	Eurocode recommendation	UK decision
6.5.6 (3)	Value of $k_2$	0.9	1.0
6.5.7 (1)	Fatigue: values for $N$ and $k_1$	$N = 10^6$ cycles $k_1 = 0.85$	Use the recommended value
7.2 (2)	Value of $k_1$	0.6	Use the recommended value
7.2 (3)	Value of $k_2$	0.45	Use the recommended value
7.2 (5)	Value of $k_3$ , $k_4$ , $k_5$	$k_3 = 0.8$ $k_4 = 1.0$ $k_5 = 0.75$	Use the recommended value
7.3.1 (5)	Limitations of crack width $w_{max}$	Table 7.1N	Use Table NA.4
7.3.2 (4)	Value of $\sigma_{sq}$	$f_{t,eq}$ in accordance with 7.3.2 (2)	Use the recommended value
7.3.4 (3)	Maximum crack spacing in Expression (7.11): values for $k_3$ and $k_4$	$k_3 = 3.4$ $k_4 = 0.425$	Use the recommended value
7.4.2 (2)	Values of basic span/depth ratios	Table 7.4N	Use Table NA.5
8.2 (2)	Values of $k_1$ and $k_2$	$k_1 = 1$ mm $k_2 = 5$ mm	Use the recommended value
8.3 (2)	Minimum mandrel diameter $\phi_{min}$	Table 8.1N	Use in Table NA.6a) and Table NA.6b)
8.6 (2)	Anchorage capacity of a welded reinforcement area	$F_{t,eq} = L_d \phi \sigma_{sq} = F_{t,eq}$	Use the recommended value

8.5 (1)	Additional rules for large diameter bars: limiting bar size	$\phi_{large} > 32$ mm	$\phi_{large} > 40$ mm
	reinforcement areas		





## National Annex

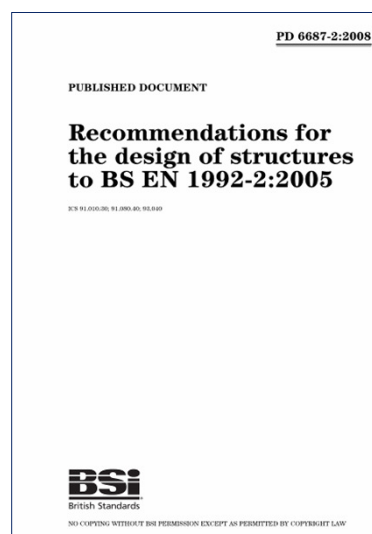
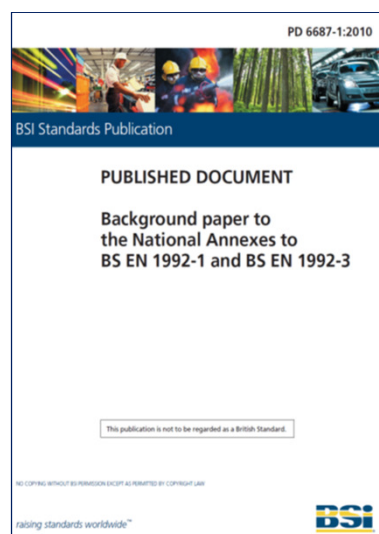
The **National Annex** provides:

- Values of Nationally Determined Parameters (NDPs)  
(NDPs have been allowed for reasons of safety, economy and durability)
  - Example: Min *diameter* for longitudinal steel in columns  
 $\phi_{\min} = 8 \text{ mm}$  in text     $\phi_{\min} = 12 \text{ mm}$  in N.A.
- The decision where main text allows alternatives
  - Example: Load arrangements in Cl. 5.1.3 (1) P
- The choice to adopt informative annexes
  - Example: Annexes E and J are not used in the UK
- Non-contradictory complementary information (NCCI)
  - Example: PD 6687 *Background paper to UK National Annexes*

In these course notes UK Nationally Determined Parameters (NDPs) are shown in blue!



## NCCI





## Features of the Eurocodes



- The Eurocodes contain Principles (P) which comprise:
  - General statements and definitions for which there is no alternative, as well as:
  - Requirements and analytical models for which no alternative is permitted
- They also contain Application Rules, which are generally rules which comply with the Principles
- The Eurocodes also use a comma (,) as the decimal marker  
(in these course notes and conventionally in the UK, the decimal marker is normally the decimal point)
- Along with all BS ENs, the Eurocodes will continue to be used during and after Brexit: no change.



## Eurocode (aka Eurocode 0 or EC0)

BS EN 1990:2002  
Basis of structural design



## Eurocode (EC0)



EN 1990 provides comprehensive information and guidance for all the Eurocodes, on the **principles and requirements for safety and serviceability**.

It gives the **partial safety factors** for actions and combinations of action for the verification of both **ultimate and serviceability limit states**.

e.g. EC0 - Ultimate load can be  $1.35 G_k + 1.5 Q_k$

## Limit State Design



*Limit states are conditions beyond which some design criterion is violated.*

Generally the structure shall be verified at:

- **Ultimate Limit State:**  
Any condition that concerns the safety of people or structure
- **Serviceability Limit State:**  
Corresponds to conditions in use of the structure. The limit state could be related to cracking, deformation or vibration.





## Limit State Design

### Ultimate Limit States:

Internal failure or excessive structural deformation (STR)

$$E_d \leq R_d;$$

Loss of equilibrium (EQU)

$$E_{d,dst} \leq R_{d,stab}$$

Failure or excessive deformation of ground (GEO)

Failure through time dependent effects e.g. fatigue (FAT)



## Limit State Design

### Serviceability Limit States:

Include:-

- the functioning of the structure or structural members under normal use;
- the comfort of people ;
- the appearance of the construction works,

Generally:

- a) Deformations that affect the appearance, the comfort of users, or the functioning of the structure (including the functioning of machines or services), or that cause damage to finishes or non-structural members ;
- b) Vibrations that cause discomfort to people, or – that limit the functional effectiveness of the structure ;
- c) Damage that is likely to adversely affect the appearance, the durability, or the functioning of the structure.



## Basis of Design



### Durability:

The structure shall be designed such that deterioration over its design working life does not impair the performance of the structure below that intended, having due regard to its environment and the anticipated level of maintenance.

## Verification by Partial Safety Factor Method



### Principle:

When using the partial factor method, it shall be verified that, in all relevant design situations, no relevant limit state is exceeded when design values for actions or effects of actions and resistances are used in the design models.

$$\text{i.e. } E_d \leq R_d$$

$E_d$  is the design value of the effect of actions.

$R_d$  is the design value of the corresponding resistance.



## Actions



### Actions:

$G_k$  = characteristic *permanent* action

$Q_k$  = characteristic *variable* action

## Design Value of Action



$$F_d = \gamma_f \cdot F_{rep}$$

Where:  $\gamma_f$  = **partial factor for actions**  
See NA to BS EN 1990: Table NA.A1.2

$F_{rep}$  = **representative value** of action  
 $= \psi \cdot F_k$

And:  
 $\psi$  converts the characteristic value of (a **variable**) action to the **representative value**.



## Representative Values of Variable Actions



Each variable action may take one of four representative values, the main one being the characteristic value.

Other representative values are obtained by the application of  $\psi$  factors, which can take one of four values, namely, 1.00 or  $\psi_0$  or  $\psi_1$  or  $\psi_2$ .

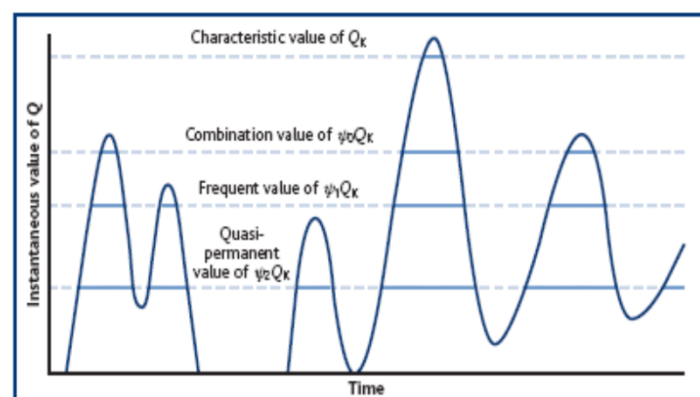
$\psi = 1.0$  when only one variable action is present in a combination.

$\psi_0 \cdot Q_k$  is the **combination value** of a variable action.

$\psi_1 \cdot Q_k$  is the **frequent value**.

$\psi_2 \cdot Q_k$  is the **quasi-permanent value**.

## Representative Values of Variable Actions



Ref: Gulvanessian, H ICE Proceedings, Civil Engineering 144 November 2001 pp.8-13



## UK Values of $\psi$ Factor



Table NA.A1.1 UK National Annex of BS EN 1990

Action	$\psi_0$	$\psi_1$	$\psi_2$
Imposed loads in buildings,			
Category A : domestic, residential	0.7	0.5	0.3
Category B : office areas	0.7	0.5	0.3
Category C : congregation areas	0.7	0.7	0.6
Category D : shopping areas	0.7	0.7	0.6
Category E : storage areas	1.0	0.9	0.8
Category F : traffic area, < 30kN	0.7	0.7	0.6
Category G : traffic area, 30 - 160kN	0.7	0.5	0.3
Category H : roofs	0.7	0	0
Snow load: $H \leq 1000$ m a.s.l.	0.5	0.2	0
Wind loads on buildings	0.5	0.2	0

## Combination of Actions



For each critical load case design values of the effects of actions are determined by combining the effects of actions that are considered to act simultaneously

Either

$$\Sigma \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10)}$$

Or (for STR and GEO) the more adverse of

$$\Sigma \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot \psi_{0,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10 a)}$$

or

$$\Sigma \xi \cdot \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10 b)}$$

↑  
The value for  $\xi$  for the UK is 0.925



## ULS (GEO/STR) for Buildings



Design values of actions, ultimate limit state - persistent and transient design situations (Table A1.2(B) Eurocode)

Comb'tion expression reference	Permanent actions		Leading variable action	Accompanying variable actions	
	Unfavourable	Favourable		Main(if any)	Others
Eqn (6.10)	$\gamma_{G,j,sup} G_{k,j,sup}$	$\gamma_{G,j,inf} G_{k,j,inf}$	$\gamma_{Q,1} Q_{k,1}$		$\gamma_{Q,i} \psi_{0,i} Q_{k,i}$
Eqn (6.10a)	$\gamma_{G,j,sup} G_{k,j,sup}$	$\gamma_{G,j,inf} G_{k,j,inf}$		$\gamma_{Q,1} \psi_{0,1} Q_{k,1}$	$\gamma_{Q,i} \psi_{0,i} Q_{k,i}$
Eqn (6.10b)	$\xi \gamma_{G,j,sup} G_{k,j,sup}$	$\gamma_{G,j,inf} G_{k,j,inf}$	$\gamma_{Q,1} Q_{k,1}$		$\gamma_{Q,i} \psi_{0,i} Q_{k,i}$

## ULS (GEO/STR) for UK Buildings



Design values of actions, ultimate limit state - persistent and transient design situations (Table A1.2(B) Eurocode)

Comb'tion expression reference	Permanent actions		Leading variable action	Accompanying variable actions	
	Unfavourable	Favourable		Main(if any)	Others
Eqn (6.10)	$1.35 G_k$	$1.0 G_k$	$1.5 Q_{k,1}$		$1.5 \psi_{0,i} Q_{k,i}$
Eqn (6.10a)	$1.35 G_k$	$1.0 G_k$		$1.5 \psi_{0,1} Q_k$	$1.5 \psi_{0,i} Q_{k,i}$
Eqn (6.10b)	$0.925 \times 1.35 G_k$	$1.0 G_k$	$1.5 Q_{k,1}$		$1.5 \psi_{0,i} Q_{k,i}$

For buildings Exp (6.10) is usually used:  $1.35 G_k + 1.5 Q_k$

But Exp (6.10b) could be used and for one variable action:  $1.25 G_k + 1.5 Q_k$

Provided:

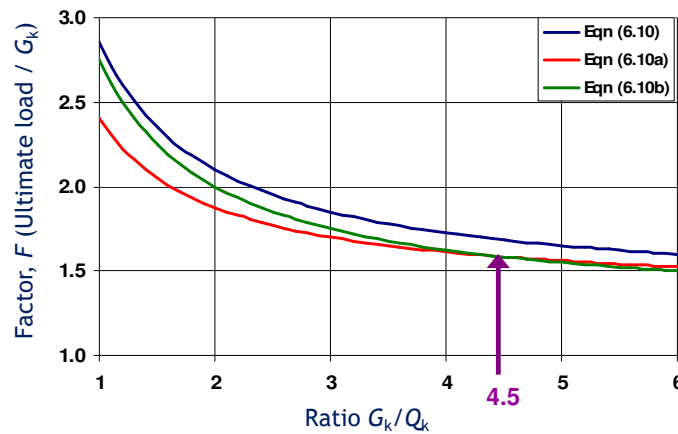
1. Permanent actions < 4.5 x variable actions
2. Excludes storage loads



## ULS (GEO/STR) for UK Buildings



Should you use Exp (6.10), (6.10a) or (6.10b)?



## Poll: ULS Load Combinations (STR)



For an office slab,

- Dead load = 6.25 kN/m<sup>2</sup>,
- Superimposed dead load = 1.5 kN/m<sup>2</sup> and
- Imposed load = 5.0 kN/m<sup>2</sup>.

What is  $n$  (ultimate load) in kN/m<sup>2</sup> ?

- a 15.7 kN/m<sup>2</sup>
- b 15.9 kN/m<sup>2</sup>
- c 17.2 kN/m<sup>2</sup>
- d 18.0 kN/m<sup>2</sup>
- e 18.9 kN/m<sup>2</sup>
- f 19.1 kN/m<sup>2</sup>



## Poll: ULS Load Combinations (STR)



For an office slab,

- DL = 6.25 kN/m<sup>2</sup>,
- SDL = 1.5 kN/m<sup>2</sup> and
- IL = 5.0 kN/m<sup>2</sup>.

What is n (ultimate load) in kN/m<sup>2</sup> ?

- a 15.7 kN/m<sup>2</sup>
- b 15.9 kN/m<sup>2</sup>
- c 17.2 kN/m<sup>2</sup>
- d 18.0 kN/m<sup>2</sup>
- e 18.9 kN/m<sup>2</sup>
- f 19.1 kN/m<sup>2</sup>

## Poll: ANSWER ULS Load Combinations (STR)



For an office slab,

What is n (ultimate load in kN/m<sup>2</sup>)?

d	Exp(6.10)				
	DL	6.25	1.35	8.44	
	SDL	1.50	1.35	2.03	
	IL	5.00	1.50	7.50	18.0
a	Exp(6.10a)				
	DL	6.25	1.35	8.44	
	SDL	1.50	1.35	2.03	
	IL	5.00	1.05	5.25	15.7
c	Exp(6.10b)				
	DL	6.25	1.25	7.81	
	SDL	1.50	1.25	1.88	
	IL	5.00	1.50	7.50	17.2
f	Wrong 1				
	DL	6.25	1.50	9.38	
	SDL	1.50	1.50	2.25	
	IL	5.00	1.50	7.50	19.1
b	Wrong 2				
	DL	6.25	1.25	7.81	
	SDL	1.50	1.25	1.88	
	IL	5.00	1.25	6.25	15.9
e	Wrong 3 (BS8110!)				
	DL	6.25	1.40	8.75	
	SDL	1.50	1.40	2.10	
	IL	5.00	1.60	8.00	18.9



**Example:****ULS Combination of Actions (STR)**

e.g: Perm. action + leading variable action + accompanying action

e.g: Dead + Imposed load (Office) + wind

The ultimate (STR) design load is either:

$$\Sigma \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10)}$$

or the more adverse of:

$$\Sigma \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot \psi_{0,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10 a)}$$

or

$$\Sigma \xi \cdot \gamma_{G,j} \cdot G_{k,j} + \gamma_{Q,1} \cdot Q_{k,1} + \Sigma \gamma_{Q,i} \cdot \psi_{0,i} \cdot Q_{k,i} \quad \text{Exp. (6.10 b)}$$

**Example:****ULS Combination of Actions (STR)**

Partial Factors for Actions (ULS)

$$\gamma_G = 1.35 \quad (\text{NA 2.2.3.3 and Table NA.A1.2})$$

$$\gamma_Q = 1.5 \quad (\text{NA 2.2.3.3 and Table NA.A1.2})$$

Relevant  $\psi$  factors

$$\psi_0 - \text{office areas} = 0.7 \quad (\text{Table NA.A.A1.1})$$

$$\psi_0 - \text{wind} = 0.5 \quad (\text{Table NA.A.A1.1})$$

The value for  $\xi$  for the UK is 0.925



## ULS Combination of Actions (STR) The Concrete Centre

### Summary

The ultimate (STR) design load is either:

$$\sum \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1} + \sum \gamma_{Q,i} \psi_{0,i} Q_{k,i} \quad \text{Exp. (6.10)}$$

$$= 1.35 G_k + 1.5 Q_{k,1} + 1.5 \times 0.5 Q_{k,w} \quad \text{Exp. (6.10)}$$

$$= 1.35 G_k + 1.5 Q_{k,1} + 0.75 Q_{k,w} \quad \text{Exp. (6.10)}$$

Or the more adverse of

$$\sum \gamma_{G,j} G_{k,j} + \gamma_{Q,1} \psi_{0,1} Q_{k,1} + \sum \gamma_{Q,i} \psi_{0,i} Q_{k,i} \quad \text{Exp. (6.10 a)}$$

$$= 1.35 G_k + 1.5 \times 0.7 Q_{k,1} + 1.5 \times 0.5 Q_{k,w} \quad \text{Exp. (6.10 a)}$$

$$= 1.35 G_k + 1.05 Q_{k,1} + 0.75 Q_{k,w} \quad \text{Exp. (6.10 a)}$$

or

$$\sum \xi_j \gamma_{G,j} G_{k,j} + \gamma_{Q,1} Q_{k,1} + \sum \gamma_{Q,i} \psi_{0,i} Q_{k,i} \quad \text{Exp. (6.10 b)}$$

$$= 0.925 \times 1.35 G_k + 1.5 Q_{k,1} + 1.5 \times 0.5 Q_{k,w} \quad \text{Exp. (6.10 b)}$$

$$= 1.25 G_k + 1.5 Q_{k,1} + 0.75 Q_{k,w} \quad \text{Exp. (6.10 b)}$$

## ULS Equilibrium (EQU) The Concrete Centre

Eurocode:


Design values of actions, ultimate limit state - persistent and transient design situations (Table A1.2(B) Eurocode)					
Comb'tion expression reference	Permanent actions		Leading variable action	Accompanying variable actions	
	Unfavourable	Favourable		Main(if any)	Others
Eqn (6.10)	$\gamma_{G,j,sup} G_{k,j,sup}$	$\gamma_{G,j,inf} G_{k,j,inf}$	$\gamma_{Q,1} Q_{k,1}$		$\gamma_{Q,i} \psi_{0,i} Q_{k,i}$

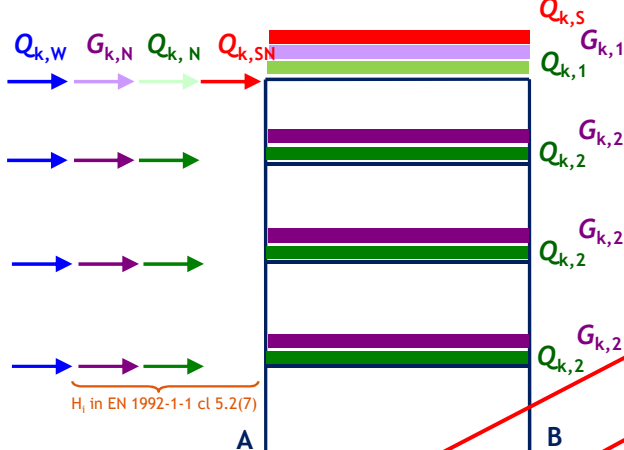
UK:

Eqn (6.10)	1.10 $G_k$	0.9 $G_k$	1.5 $Q_{k,1}$		1.5 $\psi_{0,i} Q_{k,i}$
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## Frames and EQU





$\psi_0 = 0.7$  for  $Q_{k,2}$   
 $\psi_0 = 0.7$  for  $Q_{k,1}$   
 $\psi_0 = 0.5$  for  $Q_{k,W}$   
 $\psi_0 = 0.7$  for  $Q_{k,S}$

Wind as leading variable action

Wind as accompanying variable action

**Check uplift at A**


①  $0.9 G_{k,1} + 0.9 \sum G_{k,2} - 1.5 Q_{k,W} - 1.5 \times 0.7 Q_{k,SN} - 1.10^{\#} G_{k,N} - 1.5 \times 0.7 Q_{k,N}$

②  $0.9 G_{k,1} + 0.9 \sum G_{k,2} - 1.5 \times 0.5 Q_{k,W} + 1.5 Q_{k,SN} - 1.10^{\#} G_{k,N} - 1.5 \times 0.7 Q_{k,N}$

Note # According to note in BS EN 1990 Table A.1.2 (A) & UK NA, as an alternative  $\gamma_{G, sup} = 1.35$

## SLS: Serviceability Limit State

### BS EN 1990 (6.5.3)



**Partial Factors for Actions (SLS)**

$\gamma_G = 1.00$

$\gamma_Q = 1.00$  . . . . . Subject to

$\psi_0$  - combination value  
 $\psi_1$  - frequent value.  
 $\psi_2$  - quasi-permanent value.

**So: Combinations of Actions (SLS)**

Characteristic combination (typically irreversible limit states)	$G_{k,j} + Q_{k,1} + \sum \psi_{0,i} Q_{k,i}$
Frequent combination (typically reversible limit states)	$G_{k,j} + \psi_{1,1} Q_{k,1} + \sum \psi_{2,i} Q_{k,i}$
Quasi permanent combination (typically long term effects and appearance of the structure)	$G_{k,j} + \sum \psi_{2,i} Q_{k,i}$



## UK Values of $\psi$ Factors (again)



Table NA.A1.1 UK National Annex of BS EN 1990

Action	$\psi_0$	$\psi_1$	$\psi_2$
Imposed loads in buildings,			
Category A : domestic, residential	0.7	0.5	0.3
Category B : office areas	0.7	0.5	0.3
Category C : congregation areas	0.7	0.7	0.6
Category D : shopping areas	0.7	0.7	0.6
Category E : storage areas	1.0	0.9	0.8
Category F : traffic area, < 30kN	0.7	0.7	0.6
Category G : traffic area, 30 - 160kN	0.7	0.5	0.3
Category H : roofs	0.7	0	0
Snow load: $H \leq 1000$ m a.s.l.	0.5	0.2	0
Wind loads on buildings	0.5	0.2	0

## Poll: SLS Load Combination



For an office slab,

- DL = 6.25 kN/m<sup>2</sup>,
- SDL = 1.5 kN/m<sup>2</sup> and
- IL = 5.0 kN/m<sup>2</sup>.

What is the quasi permanent load?  
in kN/m<sup>2</sup> ?

- a 9.3 kN/m<sup>2</sup>
- b 10.3 kN/m<sup>2</sup>
- c 11.3 kN/m<sup>2</sup>
- d 12.8 kN/m<sup>2</sup>
- e 15.3 kN/m<sup>2</sup>



## Poll: SLS Load Combination



For an office slab,

- DL = 6.25 kN/m<sup>2</sup>,
- SDL = 1.5 kN/m<sup>2</sup> and
- IL = 5.0 kN/m<sup>2</sup>.

What is the quasi permanent load?  
in kN/m<sup>2</sup> ?

	$\psi_2$	a	<u>9.3 kN/m<sup>2</sup></u>
$= \gamma_G * DL + \gamma_G * SDL + \psi_2 * IL$	$\psi_1$ (freq.)	b	10.3 kN/m <sup>2</sup>
$= 1.0 * 6.25 + 1.0 * 1.5 + 0.3 * 5.0$	$\psi_0$ (??)	c	11.3 kN/m <sup>2</sup>
$= 9.25 \text{ kN/m}^2$	Char.	d	12.8 kN/m <sup>2</sup>
	Wrong	e	15.3 kN/m <sup>2</sup>

## Load cases BS EN 1990 3.5(3)



“The verifications shall be carried out for all relevant design situations and load cases.”

Simplified load arrangements for beams and slabs  
are in EC2 and the NA



**NB:****There are also Partial Factors in EC7 - Geotechnical design**

The UK National Annex to EC7 refers only to Design Approach 1. Two combinations of partial load and partial soil factors need consideration.

	Partial load factor		Partial material factor, $\gamma_m$		
	$\gamma_{Gk}$	$\gamma_{Qk}$	$\tan \phi'$	$c'$	$c_u$
Combination 1	1.35	1.5	1.0	1.0	1.0
Combination 2	1.0	1.3	1.25	1.25	1.4

Note: where variable action is favourable  $\gamma_Q = 0$

$\phi'$  angle of shearing resistance (in terms of effective stress)

$c'$  cohesion intercept (in terms of effective stress)

$c_u$  undrained shear strength

These will be covered in Lecture 10



## Eurocode 2 Loads Cases

BS EN 1992

Concrete Structures



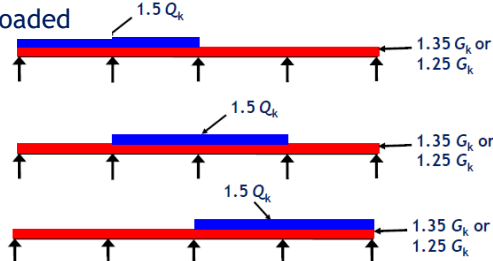
## EC2: Load cases & combinations



EC2: Cl 5.1.3 gives one 'simplified' option:

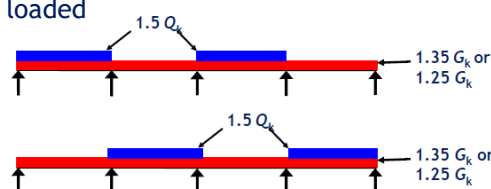
Concise: 5.4.2

Adjacent spans loaded



and

Alternate spans loaded



## UK NA to EN 1992-1-1: Simplified load arrangements



Table NA.1 — UK decisions for Nationally Determined Parameters described in BS EN 1992-1-1:2004 (continued)

Subclause	Nationally Determined Parameter	Eurocode <sup>®</sup> recommendation	UK decision
4.4.1.3 (4)	Values of $k_1$ and $k_2$	$k_1 = 40 \text{ mm}$ $k_2 = 75 \text{ mm}$	Use the recommended values $\text{EN}$
5.1.3 (1)P	Simplified load arrangements	The following load arrangements should be considered: a) alternate spans carrying the design variable and permanent load ( $\gamma_Q Q_k + \gamma_G G_k + P_{\text{im}}$ ), other spans carrying only the design permanent load $\gamma_G G_k + P_{\text{im}}$ ; b) any two adjacent spans carrying the design variable and permanent loads ( $\gamma_Q Q_k + \gamma_G G_k + P_{\text{im}}$ ); all other spans carrying only the design permanent load, $\gamma_G G_k + P_{\text{im}}$ .	Use any of the following three options. a) Consider the two load arrangements recommended in the Eurocode for alternate and adjacent spans. b) Consider the two following arrangements for all spans and alternate spans: 1) all spans carrying the design variable and permanent load ( $\gamma_Q Q_k + \gamma_G G_k + P_{\text{im}}$ ); 2) alternate spans carrying the design variable and permanent load ( $\gamma_Q Q_k + \gamma_G G_k + P_{\text{im}}$ ), other spans carrying only the design permanent load $\gamma_G G_k + P_{\text{im}}$ ; the same value of $\gamma_G$ should be used throughout the structure; c) For slabs, use the all spans loaded arrangement described in b) 1) if: 1) in a one-way spanning slab the area of each bay exceeds $30 \text{ m}^2$ ; 2) the ratio of the variable load $Q_k$ to the permanent load $G_k$ does not exceed 1.25; and 3) the variable load $Q_k$ does not exceed $5 \text{ kN/m}^2$ excluding partitions. In option c), when analysis is carried out using the load arrangement described in b) 1), the resulting support moments except those at the supports of cantilevers should be reduced by 20%, with a consequential increase in the span moments. In this context a bay means a strip across the full width of a structure bounded on the other two sides by lines of support. The load arrangements in a), b) and c) are drafted using BS EN 1990:2002, Expression (6.10). Although not shown here, they can also be drafted using BS EN 1990:2002, Expressions (6.10a) and (6.10b).
5.2 (5)	Value of $\theta_0$	1/200	Use the recommended value

<sup>EN</sup> Table NA.1 relates to BS EN 1992-1-1 incorporating Corrigendum No. 1 (January 2008),  $\text{EN}$



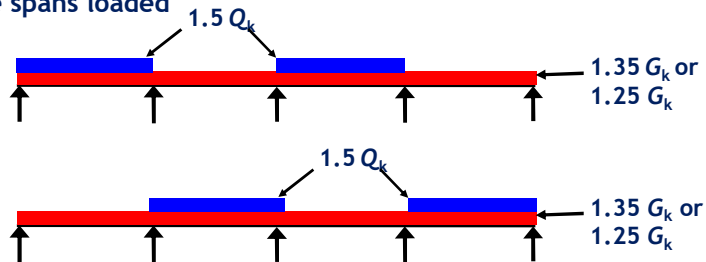
## UK NA: Simplified load arrangements



NA gives additional options, either:

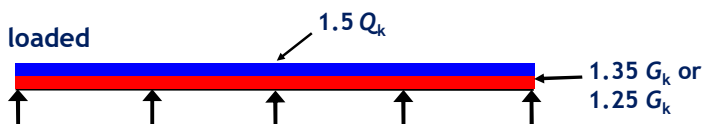
Concise: 5.4.2

Alternate spans loaded



and

All spans loaded



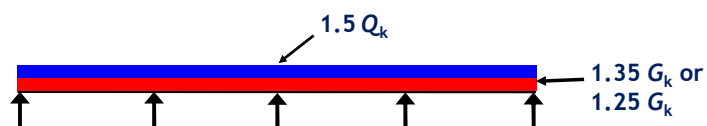
## UK NA: Arrangement of Actions



Or, for some slabs, the NA gives a 3<sup>rd</sup> option :

Concise: 5.4.2

Option 3 is all spans loaded:



You can use this option for slabs if:

1. In a one-way spanning slab the area of each bay exceeds 30m<sup>2</sup>;
2. the ratio of the variable load  $Q_k$  to the permanent load  $G_k$  does not exceed 1.25; and
3. the variable load  $Q_k$  does not exceed 5 kN/m<sup>2</sup> excluding partitions.

Note: the resulting support moments except those at the supports of cantilevers should be reduced by 20%, with a consequential increase in the span moments.



## Pattern Loading



From EN1990:

### Table A1.2(B) - Design values of actions (STR/GEO) (Set B)

NOTE 3 The characteristic values of all permanent actions from one source are multiplied by  $\gamma_{G,sup}$  if the total resulting action effect is unfavourable and  $\gamma_{G,inf}$  if the total resulting action effect is favourable. For example, all actions originating from the self weight of the structure may be considered as coming from one source; this also applies if different materials are involved.

There is no such note for **Table A1.2(A) - Design values of actions (EQU) (Set A)**

Therefore there should be **no pattern loading on permanent actions for STR and GEO** verifications but there should be pattern loading on permanent actions for EQU.



## Eurocode 1 - Loads/Actions

BS EN 1991

Actions on structures



## Eurocode 1



Eurocode 1 has ten parts:

- 1991-1-1 Densities, self-weight and imposed loads
- 1991-1-2 Actions on structures exposed to fire
- 1991-1-3 Snow loads
- 1991-1-4 Wind actions
- 1991-1-5 Thermal actions
- 1991-1-6 Actions during execution
- 1991-1-7 Accidental actions due to impact and explosions
- 1991-2 Traffic loads on bridges
- 1991-3 Actions induced by cranes and machinery
- 1991-4 Actions in silos and tanks

## EN 1991-1-1



Densities, self-weight and imposed loads

- Bulk density of mass concrete is  $24 \text{ kN/m}^3$
- Bulk density of *reinforced* concrete is  $25 \text{ kN/m}^3$ 
  - This represents 1.84% reinforcement
- Add  $1 \text{ kN/m}^3$  for wet concrete
- The UK NA uses the same loads as BS 6399
- Plant loading not given



## EN 1991-1-1: extracts from UK NA



Category	Example Use	$q_k$ (kN/m <sup>2</sup> ) Char. value of udl	$Q_k$ (kN) Char. value of pt load
A1	All uses within self-contained dwelling units	1.5	2.0
A2	Bedrooms and dormitories	1.5	2.0
A3	Bedrooms in hotels and motels, hospital wards and toilets	2.0	2.0
A5	Balconies in single family dwelling units	2.5	2.0
A7	Balconies in hotels and motels	4.0 min	2.0
B1	Offices for general use	2.5	2.7
C5	Assembly area without fixed seating, concert halls, bars, places of worship	5.0	3.6
D1/2	Shopping areas	4.0	3.6
E12	General storage	2.4 per m ht	7.0
E17	Dense mobile stacking in warehouses	4.8 per m ht (min 15.0)	7.0
F	Gross vehicle weight $\leq 30$ kN	2.5	10.0

## EN 1991-1-1



Imposed load reductions:

### CI 6.3.1.2 (10 & 11)

EC1 allows imposed load reductions for large floor areas and several storeys. The NA modifies the equation in EC1: use [either](#):

$$\alpha_A = 1.0 - A/1000 \geq 0.75 \quad (\text{NA.1})$$

where A is the area (m<sup>2</sup>) supported

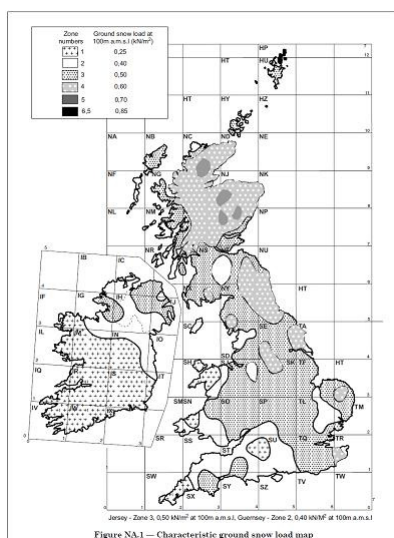
[or](#)

$$\begin{aligned} \alpha_n &= 1.1 - n/10 & 1 \leq n \leq 5 \\ \alpha_n &= 0.6 & 6 \leq n \leq 10 \\ \alpha_n &= 0.5 & n > 10 \end{aligned} \quad (\text{NA.2})$$

where n is the number of storeys supported



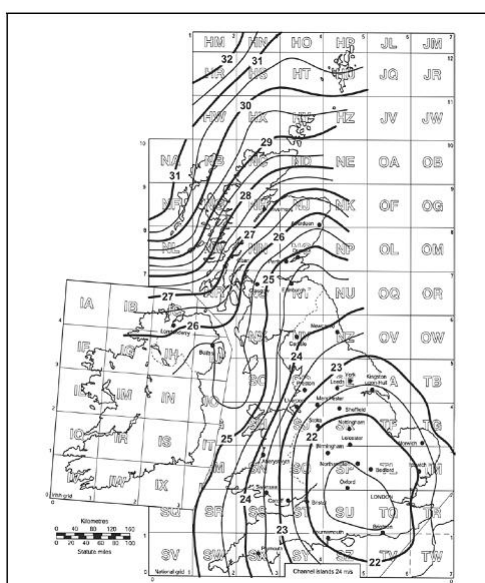
## BS EN 1991-3 (NA) Snow



Zone numbers	Ground snow load at 100m a.m.s.l (kN/m <sup>2</sup> )
1	0,25
2	0,40
3	0,50
4	0,60
5	0,70
6,5	0,85

Snow loads

## BS EN 1991 1-4 (NA) Wind







## Exercise

### Lecture 1



### Load Arrangement Exercise

**Q1. Overhanging cantilever beam.** Determine the  $\gamma_F$  factors that should be applied to  $G_k$  and  $Q_k$ :-

- a) for equilibrium (EQU) (BS EN 1990, Table A1.2(A) & UK NA)
- b) for structural strength (STR) (BS EN 1990, Exp (6.10) & UK NA)



**Q2. Continuous single-way slab.** Assuming permanent actions = 6 kN/m<sup>2</sup> and variable actions = 4 kN/m<sup>2</sup>, calculate the most economic value of ULS total loading (kN/m<sup>2</sup>) using Exps (6.10), (6.10a) and (6.10b) (see BS EN 1990 Table A1.2(B) & UK NA).





## Load Arrangement Exercise (pro forma)



<u>Q1</u>	Span $\gamma_G G_k + \gamma_Q Q_k$	Cant $\gamma_G G_k + \gamma_Q Q_k$
a) EQU		
b1) STR		
b2) STR		



<u>Q2</u>	$\gamma_G G_k$	$\gamma_Q Q_k$	n
(6.10)			
(6.10a)			
(6.10b)			



We will go through the answers to the exercise at the beginning of next week's lecture





## End of Lecture 1

- Introduction
- Background & Basics
- Eurocode (Eurocode 0)
- Eurocode Load Combinations
- Eurocode 2 Load Cases
- Eurocode 1 Loads/Actions
- Exercise